# **Fares not fair**

## **Task description**

Pupils determine whether the rates for taxi fares, set by a local council, are fair in relation to the changing cost of fuel.

Suitability National Curriculum levels 6 to 8

Time45 minutes to 1 hour

**Resources** Paper and calculator

#### **Key Processes involved**

- **Analysing**: Process the data to find the relationship between fuel cost and taxi fares.
- Interpreting and evaluation: Use findings to justify their recommended fare.
- Communicating and reflecting: Communicate findings effectively and explain recommendation clearly.

## Teacher guidance

You might begin by showing the slides on a whiteboard and commenting:

- Even though taxi drivers are usually self employed, the taxi fares they can charge are not set by the drivers, but by their local Council. In 2008, taxi drivers in Surrey complained that the prices they were allowed to charge were not fair as the price of diesel fuel had gone up so much.
- The data shows the cost of fuel and the price of taxi fares over 8 years. Your task is to examine the drivers' claim and decide on a fair price for them to charge.

The task requires knowledge of proportionality.

During the task, the following probing questions may be helpful

- What method will you use to decide what would make a fair price?
- What does 'fair' mean?
- Are there different ways you could use the information to make your decision?
- The taxi drivers focus on the cost of their fuel; should there be other factors in deciding what would be a fair price?

# Fares not fair!

# Cabbies complain - "Fares are set too low"



In May 2008, taxi drivers in Surrey complained that they were not allowed to increase their taxi fares although the cost of fuel had risen.

The table shows how costs and prices have changed.

How prices chan	ged			
Average cost of one litre of diesel fuel		Taxi fare (2 mile	journey)	
May 2000	82p	May 2000	£3.50	
May 2001	79p	May 2001	£3.80	
May 2002	77p	May 2002	£3.90	
May 2003	78p	May 2003	£4.40	
May 2004	83p	May 2004	£5.00	
May 2005	90p	May 2005	£5.00	
May 2006	92p	May 2006	£5.00	
May 2007	97p	May 2007	£5.20	Fact:
May 2008	125p	May 2008	£5.20	Taud famou and a st
				by the Council

As diesel costs have increased so much, it seems reasonable that taxi fares should have been allowed to increase in May 2008.

How much would it have been reasonable to allow fares to increase?

Use the data to make your suggestion for what would be a fairer taxi fare for May 2008; Explain why.

# Assessment guidance

# **Progression in Key Processes**

Representing	Analysing	Interpreting and Evaluating	Communicating and reflecting
What is done with the data	The data processed to gain an insight into patterns and exceptions	Findings used to justify their recommended fare	Methods and findings explained throughout; insight into the problem shown
Chooses an additive method to compare changes in costs Pupil A	Recognises that a rise (or fall) in the cost of diesel is not always matched by a rise (or fall) in fares Pupil A	Gives a recommended fare	Identifies which years are being considered and explains their simplistic method clearly Pupil A
Attempts to summarise the outcomes from their additive method, eg uses averages	Makes simple statements when summarising the data, eg 'Between 2001 and 2003 diesel costs fell but fares went up'	Forms a simple argument to justify their recommended fare Pupils A and B	Identifies which years are being considered and shows the calculations that lead to a solution, thus allowing their working to be checked Pupil B
Uses a non- additive method, even if simplistic Pupils B and C + D	Processes the information to gain an insight into the data, eg by using means or percentages Pupils B and C + D	Forms more complex arguments to justify their recommended fare	Shows methods clearly in a solution that 'flows'; recognises that other factors will be applicable in determining fares Pupils C + D
Uses a non- additive method based on at least the last four years	Uses a scatter graph or other insightful methods that show the relationship between the costs of diesel and prices of fares	Uses additional mathematical tools to inform their recommended fare, eg draws a line of best fit	As above, but also justifies why the problem is complex, eg 'fuel is a small proportion of the costs so other costs, (eg labour) need to be considered'

# Sample responses

## Pupil A

Averag	e cost of o	ne litre of diesel	Cost of a taxi fai	re for a 2 mile jour
130	May 2000	82p	May 2000	£3.50
12P	May 2001	79p	May 2001	£3.80 130
nip-	May 2002	77p	May 2002	£3.90 10
140	May 2003	78p	May 2003	£4.40 A SO
P70	May 2004	83p	May 2004	£5.00 A 60
rzę.	May 2005	90p	May 2005	£5.00 € OP
15e	May 2006	92p	May 2006	£5.00 \$ 0P
289	May 2007	97p	May 2007	E5.20 1 20P
	May 2008	125p = about	S2% 01 May 2008	E5.20 \$ 0P

Because in May 2000, they got £3.50 and the price of petrol was SZP. Now that petrol has increased 43p, their pay should increase by about SOP - which would take their pay to £4.00. Also, they have to pay tor food and they should have given some money for food and drink - bringing it up to £5.40.

### Comments

Pupil A starts with the changes per year in fuel costs and fares, but there is little evidence of insight into the values found. He works out the percentage increase in the fuel costs from 2000 to 2008 – but shows it as 52% not 152%. He does not use this, but reverts to using the cost difference between May 2000 and 2008. He shows an awareness that real life costs are based on more than the price of fuel, but the solution is simplistic and not justified.

#### **Probing questions and feedback**

• You worked out a percentage change; your solution would have been better if you had used that, ie by finding 52% of £3.50 and adding the answer to £3.50. You suggest £1.40 for food and drink, but why should that suddenly appear for 2008?

This pupil would benefit from tasks that probe his ability to reason mathematically. Working with another pupil might encourage him to reflect on his methods and his solutions.

## Pupil B

My reasons: I Look at 200 the diffrence between 2006 and 2007. The diffrence in fuel was sp'and, the diffrence in taxi pares was 20p. So every 5p the ç vel goes up the taxi pares Shald go up Zap. The diffrence in ,200 from 2001 in fuel was ZSp. there are 5,55 in 28 . So that up£1.00.~ means the fuel Should 90 Then with the 3 Left over, a Of 20 is i added five S. \$ So pence. total EO which brund my

### Comments

Pupil B has used the change from 2006 to 2007 to inform his solution for 2008, but with no reference to the period before 2006. He uses proportional reasoning, but his understanding of fractions is insufficient to complete the method since he calculates one quarter of 20p rather than three-fifths of 20p.

#### **Probing questions and feedback**

- When solving a complex problem, remember to show evidence for your thinking; for example, why did you choose to work only with 2006, 2007 and 2008; what about earlier years?
- Why did you choose that particular method?

Practice at interpreting data sets would benefit this pupil, as would working with contexts that require an understanding of fractions.

# Pupils C and D

How prices changed	
Average cost of one litre of diesel Cost	it of a taxi fare for a 2 mile journey
May 2000 82p	May 2000 £3.50 300
May 2001 79p	May 2001 £3.80
May 2002 77p - 2p	May 2002 £3.90
May 2003 78p	May 2003 £4.40 000
May 2004 83p Sp	May 2004 £5.00 60P
May 2005 90p 7p	May 2005 £5.00 P
May 2006 92p 2P	May 2006 £5.00 04 Fact:
May 2007 97p Sp	May 2007 £5.20 Z OP Taxi fares are set
May 2008 125p 28p	May 2008 £5.20 Op by the Council
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The second second second second	Change _ im
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3.90 2002 - 0.79-1	2.77:002
0.02 .00- 0-	$-\alpha$ $(2\alpha P)$
0.79×10= 2.5	3/0
4.40 0000 - 01	1
2003 - 0:01 -0	$3,77 \times 100 = 1.30 / a$
son contra posico	Relation of the of
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	the to show with the power
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	the second
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	0.82 - 52.44%
fare - 2000-2008	
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	3.5 2100 - 40.376
52.44 % OC YTE.	50 - 12 20
THE REAL	
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	dianal in the many 2000 June of
	change is
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	you we want the second se
	- The price difference) and (20) lie 57%
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	NOT EQUAL - The taxi drivers are cosen. We then jourd 52.44% of 23.50 We then pound 52.44% of 23.50
	NOT EQUAL - The taxi drivers are cosen We then found 52.44% of 23.50 (the May 2000 price) which is 22.30.
	NOT EQUAL - The taxi drivers are cosine We then found 52.44% of 23.50 (the May 2000 price) which is 22.30. We then added that to the price of
	Not Eaurel - The taxi drivers are cosine we then found 52.44% of 23.50 (the May 2000 price) which is $22.30$ . We then added that to the price of (and in 2000 (72.50).
	NOT EQUAL - The taxi drivers are cosine We then jound 52.44% of 23.50 (The May 2000 price) which is 22.30. We then added that to the price of Janes in 2000 (23.50).
	NOT EQUAL - The taxi drivers are cosine We then found 52.44% of 23.50 (The May 2000 price) which is 22.30. We then added that to the price of fares in 2000 (23.50). So the Near amount that, the taxi
	NOT EQUAL - The taxi drivers are cosine We then found 52.44% of \$3.50 (the May 2000 price) which is \$2.30. We then added that to the price of Jares in 2000 (\$3.50). So the near amount that the taxi fare should be is \$5.80

### Comments

Pupils C and D start by using differences in costs, but change to percentages. They find the percentage change for several years decide not to continue; their oral explanation was that: 'there isn't a pattern in the data, you can't see anything, so we think if we just work out what is happening from the beginning it will be simpler and clearer'. They then use their multiplicative method to compare how prices have changed from 2000 to 2007 and apply their findings to 2008 to find a justified conclusion. Most calculations are accurate, but not all. Their communication is clear, although there is no evidence of reflection on the task.

### **Probing questions and feedback**

• When working on a complex problem, try to think about how well the mathematical model you are applying fits the real life situation; in this task you could have thought about whether basing the cost of a taxi fare only on the cost of diesel was appropriate.

These pupils enjoyed working on the task, seeing it as an exciting challenge. Providing them with extended open-ended tasks, such as a Bowland case study, would capitalise on this enthusiasm and should enable them to develop their skills further.